

① Bestimme jeweils die Lösungsmenge der Gleichung (Grundmenge \mathbb{R}).

- | | | |
|--------------------------------------|---|---|
| a) $\{-5; 9\}$ | b) $\{4; 6\}$ | c) $\{-3\}$ |
| d) $\{6; 8\}$ | e) $\{1 - \sqrt{2}; 1 + \sqrt{2}\}$ | f) $\{3 - \sqrt{2}; 3 + \sqrt{2}\}$ |
| g) $\{-11; -12\}$ | h) $\{\}$ | i) $\{\frac{1}{2}; 2\}$ |
| j) $\{\frac{2}{3}; 1\}$ | k) $\{\}$ | l) $\{-\frac{1}{2}; 4\}$ |
| m) $\{\frac{4}{3}; 5\}$ | n) $\{\}$ | o) $\{-\frac{2}{3}\}$ |
| p) $\{\frac{5}{3}; \frac{3}{4}\}$ | q) $\{-\frac{1}{3}; \frac{2}{3}\}$ | r) $\{-1; \frac{4}{5}\}$ |
| s) $\{-\frac{1}{4}; \frac{1}{2}\}$ | t) $\{2\sqrt{2} - 2; 2\sqrt{2} + 2\}$ | u) $\{\sqrt{3}\}$ |
| v) $\{-1 - \sqrt{2}; 1 - \sqrt{2}\}$ | w) $\{\sqrt{2} - \sqrt{3}; \sqrt{2} + \sqrt{3}\}$ | x) $\{\sqrt{2}; -\frac{1}{2}\sqrt{2}\}$ |
| y) $\{\sqrt{2}; 2\sqrt{2}\}$ | z) $\{-100; 0,1\}$ | |

② ...und weiter geht's:

- | | | |
|---|---|---------------------------------------|
| a) $\{-\frac{1}{5}; 200\}$ | b) $\{-25; 2\frac{1}{2}\}$ | c) $\{-3,3; 33\}$ |
| d) $\{-222; 111\}$ | e) $\{-2; \frac{1}{2}\}$ | f) $\{-2; -\frac{1}{4}\}$ |
| g) $\{-\frac{1}{4}; \frac{1}{2}\}$ | h) $\{-\frac{1}{2}(1 + \sqrt{5}); -\frac{1}{2}(1 - \sqrt{5})\}$ | i) $\{2 - \sqrt{3}; 2 + \sqrt{3}\}$ |
| j) $\{1 - \frac{3}{2}\sqrt{2}; 1 + \frac{3}{2}\sqrt{2}\}$ | k) $\{\frac{1}{2}\}$ | l) $\{\}$ |
| m) $\{-1; 4\}$ | n) $\{\}$ | o) $\{-\frac{8}{3}; 0\}$ |
| p) $\{0; \frac{1}{2}\}$ | q) $\{-3\frac{1}{2}; 3\frac{1}{2}\}$ | r) $\{0; \frac{3}{7}\}$ |
| s) $\{-\frac{\sqrt{39}}{3}; \frac{\sqrt{39}}{3}\}$ | t) $\{-3; \frac{5}{3}\}$ | u) $\{-0,4; \frac{3}{4}\}$ |
| v) $\{-\frac{3}{4}; \frac{2}{5}\}$ | w) $\{\}$ | x) $\{2 - \sqrt{41}; 2 + \sqrt{41}\}$ |
| y) $\{-\frac{1}{4}; -\frac{1}{8}\}$ | z) $\{37; 63\}$ | |

③ ...und die dritte Runde:

- | | | |
|--------------------------------------|---|---|
| a) $\{-23; 17\}$ | b) $\{-123; 23\}$ | c) $\{-\frac{3}{7}; 49\}$ |
| d) $\{-\frac{4}{13}; 78\}$ | e) $\{-4; -\frac{43}{13}\}$ | f) $\{\frac{7}{13}\}$ |
| g) $\{-2\frac{1}{2}; 2\frac{1}{2}\}$ | h) $\{-8\frac{1}{2}; \frac{1}{4}\}$ | i) $\{-3\frac{1}{2}; \frac{1}{2}\}$ |
| j) $\{-1; \frac{11}{3}\}$ | k) $\{5 - \frac{1}{2}\sqrt{138}; 5 + \frac{1}{2}\sqrt{138}\}$ | l) $\{\frac{1}{2} - \sqrt{7}; \frac{1}{2} + \sqrt{7}\}$ |
| m) $\{3\sqrt{3}; 5\sqrt{3}\}$ | n) $\{-\sqrt{2}; 3\sqrt{2}\}$ | o) $\{\sqrt{2} - \sqrt{3}; \sqrt{2} + \sqrt{3}\}$ |
| p) $\{2\sqrt{5}\}$ | q) $\{4\sqrt{3}\}$ | r) $\{\}$ |
| s) $\{\sqrt{3}; 2\sqrt{3}\}$ | t) $\{-\frac{5}{2}\sqrt{2}; \frac{1}{4}\sqrt{2}\}$ | u) $\{-4 - 2\sqrt{2}; 4 - 2\sqrt{2}\}$ |
| v) $\{\sqrt{5} - 3; \sqrt{5} + 3\}$ | w) $\{-\sqrt{2} - 3; -\sqrt{2} + 3\}$ | x) $\{\sqrt{3} - 3; \sqrt{3} + 3\}$ |
| y) $\{1 - \sqrt{2}; 3 + \sqrt{2}\}$ | z) $\{-1; \sqrt{3}\}$ | |

④ Löse mithilfe einer geeigneten Substitution:

- | | | |
|--|---|---|
| a) $\{-3; 3\}$ | b) $\{-3; 3\}$ | c) $\{\}$ |
| d) $\{-\frac{1}{2}\sqrt{2}; \frac{1}{2}\sqrt{2}\}$ | e) $\{-\sqrt{5}; 0; \sqrt{5}\}$ | f) $\{\}$ |
| g) $\{-1\frac{1}{2}; -1; 1; 1\frac{1}{2}\}$ | h) $\{-\sqrt{3}; -\sqrt{2}; \sqrt{2}; \sqrt{3}\}$ | i) $\{-\frac{1}{2}\sqrt{2}; \frac{1}{2}\sqrt{2}\}$ |
| j) $\{-\sqrt{2}; \sqrt{2}\}$ | k) $\{-\frac{1}{2}; -\frac{1}{3}; \frac{1}{3}; \frac{1}{2}\}$ | l) $\{-\frac{3}{2}; -\frac{2}{3}; \frac{2}{3}; \frac{3}{2}\}$ |
| m) $\{-1; 2\}$ | n) $\{2; 3\}$ | o) $\{-2; -1; 1; 2\}$ |
| p) $\{9; 49\}$ | q) $\{16; 49\}$ | r) $\{16\}$ |
| s) $\{\sqrt{2} + 1; \sqrt{2} - 1\}$ | t) $\{2 - \sqrt{3}; 2 + \sqrt{3}\}$ | |
| u) $\{0; 19\}$ | v) $\{-4; -1; 1; 4\}$ | |
| w) $\{-\sqrt{2}; \sqrt{2}\}$ | x) $\{-2; 2\}$ | |
| y) $\{\frac{1}{2}; 2\}$ | z) $\{2\}$ | |

⑤ Karneval der Gleichungen:

- | | | |
|--|--------------------------------|-------------------------|
| a) $\{4; 24\}$ | b) $\{0; \frac{1}{2}\}$ | |
| c) $\{1; 5\}$ | | |
| d) $\{-5; 6\}$ | e) $\{0; 1\}$ | |
| f) $\{-\sqrt{7}; \sqrt{7}\}$ | g) $\{\frac{3}{4}\sqrt{2}-1\}$ | |
| h) $\{\frac{1}{2}\sqrt{2}; \sqrt{2}\}$ | | |
| i) $\{4\}$ | j) $\{\}$ | |
| k) $\{1 - \sqrt{3}; 1 + \sqrt{3}\}$ | l) $\{1\frac{3}{5}; 5\}$ | |
| m) $\{-\sqrt{2}; \sqrt{2}\}$ | n) $\{\}$ | |
| o) $\{85\}$ | p) $\{2; 3\}$ | q) $\{\frac{3}{4}; 4\}$ |
| r) $\{-2; -3\}$ | s) $\{-3; 6\}$ | t) $\{2\}$ |
| u) $\{-2\}$ | v) $\{\}$ | w) $\{2\}$ |
| x) $\{-4; 4\}$ | y) $\{\sqrt{2}\}$ | z) $\{12\}$ |